

# Poly[diaquabis( $\mu_3$ -1H-imidazole-4,5-dicarboxylato)( $\mu_2$ -sulfato)-diytterbium(III)]

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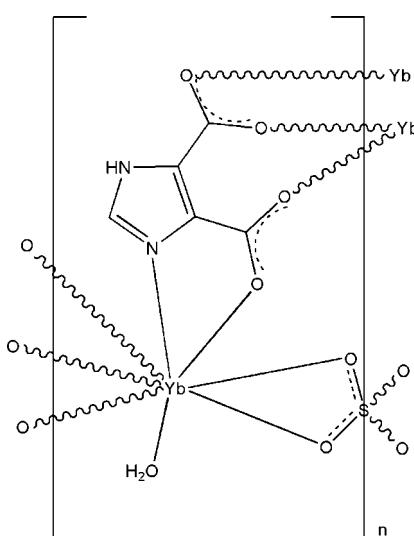
Received 24 October 2011; accepted 31 October 2011

Key indicators: single-crystal X-ray study;  $T = 296$  K; mean  $\sigma(\text{C}-\text{C}) = 0.007$  Å;  $R$  factor = 0.020;  $wR$  factor = 0.047; data-to-parameter ratio = 10.2.

In the title compound,  $[\text{Yb}_2(\text{C}_5\text{H}_2\text{N}_2\text{O}_4)_2(\text{SO}_4)(\text{H}_2\text{O})_2]_n$ , the  $\text{Yb}^{\text{III}}$  ion is eight-coordinated by four O atoms and one N atom from three imidazole-4,5-dicarboxylate ligands, two O atoms from one  $\text{SO}_4^{2-}$  anion (site symmetry 2), as well as one O atom of a water molecule, giving a bicapped trigonal-prismatic coordination geometry. The metal coordination units are connected by bridging imidazole-4,5-dicarboxylate and sulfate ligands, generating a heterometallic layer. The layers are stacked along the  $a$  axis via  $\text{N}-\text{H}\cdots\text{O}$ ,  $\text{O}-\text{H}\cdots\text{O}$ , and  $\text{C}-\text{H}\cdots\text{O}$  hydrogen-bonding interactions, generating a three-dimensional framework.

## Related literature

For the application of multifunctional organic ligands containing O- and N-donors in the design of metal-organic frameworks, see: Cheng *et al.* (2006); Kuang *et al.* (2007); Sun *et al.* (2006); Zhu *et al.* (2010).



## Experimental

### Crystal data

$[\text{Yb}_2(\text{C}_5\text{H}_2\text{N}_2\text{O}_4)_2(\text{SO}_4)(\text{H}_2\text{O})_2]$	$V = 1714.7 (2)$ Å <sup>3</sup>
$M_r = 786.35$	$Z = 4$
Monoclinic, $C2/c$	Mo $K\alpha$ radiation
$a = 21.1089 (14)$ Å	$\mu = 11.05$ mm <sup>-1</sup>
$b = 6.5584 (4)$ Å	$T = 296$ K
$c = 12.8766 (9)$ Å	$0.20 \times 0.18 \times 0.15$ mm
$\beta = 105.874 (1)$ °	

### Data collection

Bruker APEXII area-detector diffractometer	4239 measured reflections
Absorption correction: multi-scan ( <i>SADABS</i> ; Sheldrick, 1996)	1534 independent reflections
$T_{\min} = 0.126$ , $T_{\max} = 0.191$	1392 reflections with $I > 2\sigma(I)$
	$R_{\text{int}} = 0.023$

### Refinement

$R[F^2 > 2\sigma(F^2)] = 0.020$	H atoms treated by a mixture of independent and constrained refinement
$wR(F^2) = 0.047$	$\Delta\rho_{\text{max}} = 0.66$ e Å <sup>-3</sup>
$S = 1.09$	$\Delta\rho_{\text{min}} = -0.99$ e Å <sup>-3</sup>
1534 reflections	
150 parameters	
4 restraints	

**Table 1**  
Hydrogen-bond geometry (Å, °).

D—H···A	D—H	H···A	D···A	D—H···A
N2—H1···O6 <sup>i</sup>	0.87 (5)	2.09 (3)	2.925 (6)	161 (5)
O1W—H2W···O2 <sup>ii</sup>	0.82 (2)	1.94 (3)	2.693 (5)	151 (5)
O1W—H1W···O3 <sup>iii</sup>	0.82 (6)	2.24 (4)	2.896 (5)	138 (5)
O1W—H1W···O4 <sup>iii</sup>	0.82 (6)	2.51 (6)	3.308 (5)	167 (5)
C5—H5···O5 <sup>iv</sup>	0.93	2.52	3.347 (6)	149
Symmetry codes: (i) $x, -y + 1, z + \frac{1}{2}$ ; (ii) $-x + \frac{1}{2}, y + \frac{1}{2}, -z + \frac{3}{2}$ ; (iii) $-x + \frac{1}{2}, -y + \frac{1}{2}, -z + 2$ ; (iv) $x, y + 1, z$ .				

Data collection: *APEX2* (Bruker, 2004); cell refinement: *SAINT* (Bruker, 2004); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *SHELXTL* (Sheldrick, 2008); software used to prepare material for publication: *SHELXL97*.

The authors acknowledge South China Normal University for supporting this work.

Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: PV2472).

## References

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## **supplementary materials**

*Acta Cryst.* (2011). E67, m1683 [doi:10.1107/S1600536811045673]

## Poly[diaquabis( $\mu_3$ -1H-imidazole-4,5-dicarboxylato)( $\mu_2$ -sulfato)diytterbium(III)]

L.-C. Zhu

### Comment

In the past few years, the application of multifunctional organic ligands containing O– and N–donors to design metal-organic frameworks are of increasing interest, not only because of their impressive topological structures, but also due to their versatile applications in ion exchange, magnetism, bimetallic catalysis and luminescent probe (Cheng *et al.*, 2006; Kuang *et al.*, 2007; Sun *et al.*, 2006; Zhu *et al.*, 2010). As an extension of this research, the structure of the title compound, a new metal-organic framework, has been determined which is presented in this article.

The asymmetric unite of the title compound (Fig. 1), contains a  $\text{Yb}^{\text{III}}$  ion, an imidazole-4,5-dicarboxylate ligand, a half  $\text{SO}_4^{2-}$  anion, and a coordinated water molecule. The  $\text{Yb}^{\text{III}}$  ion is eight-coordinated by four O atoms and a N atom from three imidazole-4,5-dicarboxylate ligands, two O atoms from a  $\text{SO}_4^{2-}$  anion as well as a coordinated water molecule, giving a bicapped trigonal prismatic coordination geometry. The metal coordination units are connected by bridging imidazole-4,5-dicarboxylate and sulfate ligands, generating a two-dimensional heterometallic layer. The two-dimensional layers are stacked along  $a$  axis via N—H···O, O—H···O, and C—H···O hydrogen-bonding interactions to generate the three-dimensional framework (Table 1 and Fig. 2).

### Experimental

A mixture of  $\text{Yb}_2\text{O}_3$  (0.099 g, 0.25 mmol), imidazole-4,5-dicarboxylic acid (0.156 g, 1 mmol), and  $\text{H}_2\text{O}$  (7 ml) was sealed in a 20 ml Teflon-lined reaction vessel at 443 K for 5 days then slowly cooled to room temperature. The product was collected by filtration, washed with water and air-dried. Colorless block crystals suitable for X-ray analysis were obtained.

### Refinement

H atoms bonded to C atoms were positioned geometrically and refined as riding, with C—H = 0.93 Å and  $U_{\text{iso}}(\text{H}) = 1.2 U_{\text{eq}}(\text{C})$ . H atoms bonded to N atoms water molecules were found from difference Fourier maps and refined isotropically with a restraint of N—H = 0.87 Å, O—H = 0.82 Å and  $U_{\text{iso}}(\text{H}) = 1.5 U_{\text{eq}}(\text{N}, \text{O})$ .

### Figures

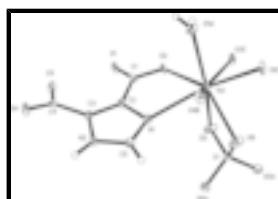


Fig. 1. The molecular structure of the title complexes showing atomic-numbering scheme and displacement ellipsoids drawn at 30% probability level. Symmetry codes: A = 1 -  $x$ ,  $y$ , 1.5 -  $z$ ; B =  $x$ , 1 -  $y$ , -1/2 +  $z$ ; C =  $x$ , - $y$ , -1/2 +  $z$ .

## supplementary materials

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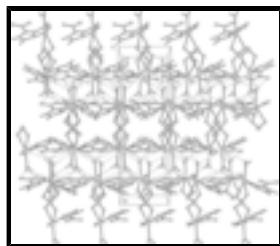


Fig. 2. A view of the three-dimensional structure of the title compound, the hydrogen bonding interactions have been drawn as broken lines.

### Poly[diaqua bis( $\mu_3$ -1*H*-imidazole-4,5-dicarboxylato)( $\mu_2$ -sulfato)diytterbium(III)]

#### Crystal data

[Yb <sub>2</sub> (C <sub>5</sub> H <sub>2</sub> N <sub>2</sub> O <sub>4</sub> ) <sub>2</sub> (SO <sub>4</sub> )(H <sub>2</sub> O) <sub>2</sub> ]	<i>F</i> (000) = 1456
<i>M<sub>r</sub></i> = 786.35	<i>D<sub>x</sub></i> = 3.046 Mg m <sup>-3</sup>
Monoclinic, <i>C</i> 2/c	Mo <i>K</i> α radiation, $\lambda$ = 0.71073 Å
Hall symbol: -C 2yc	Cell parameters from 2574 reflections
<i>a</i> = 21.1089 (14) Å	$\theta$ = 3.3–28.0°
<i>b</i> = 6.5584 (4) Å	$\mu$ = 11.05 mm <sup>-1</sup>
<i>c</i> = 12.8766 (9) Å	<i>T</i> = 296 K
$\beta$ = 105.874 (1)°	Block, colorless
<i>V</i> = 1714.7 (2) Å <sup>3</sup>	0.20 × 0.18 × 0.15 mm
<i>Z</i> = 4	

#### Data collection

Bruker APEXII area-detector diffractometer	1534 independent reflections
Radiation source: fine-focus sealed tube graphite	1392 reflections with $I > 2\sigma(I)$
$\varphi$ and $\omega$ scan	$R_{\text{int}}$ = 0.023
Absorption correction: multi-scan ( <i>SADABS</i> ; Sheldrick, 1996)	$\theta_{\text{max}} = 25.2^\circ$ , $\theta_{\text{min}} = 2.0^\circ$
$T_{\text{min}} = 0.126$ , $T_{\text{max}} = 0.191$	$h = -25 \rightarrow 22$
4239 measured reflections	$k = -7 \rightarrow 7$
	$l = -14 \rightarrow 15$

#### Refinement

Refinement on $F^2$	Primary atom site location: structure-invariant direct methods
Least-squares matrix: full	Secondary atom site location: difference Fourier map
$R[F^2 > 2\sigma(F^2)]$ = 0.020	Hydrogen site location: inferred from neighbouring sites
$wR(F^2)$ = 0.047	H atoms treated by a mixture of independent and constrained refinement
$S$ = 1.09	$w = 1/[\sigma^2(F_o^2) + (0.0216P)^2 + 5.6648P]$
1534 reflections	where $P = (F_o^2 + 2F_c^2)/3$
150 parameters	$(\Delta/\sigma)_{\text{max}} = 0.001$
	$\Delta\rho_{\text{max}} = 0.66 \text{ e \AA}^{-3}$

4 restraints

$\Delta\rho_{\min} = -0.99 \text{ e \AA}^{-3}$

### Special details

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) etc. and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

### Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )

	$x$	$y$	$z$	$U_{\text{iso}}^*/U_{\text{eq}}$
Yb1	0.355312 (10)	0.07841 (3)	0.714967 (16)	0.01086 (9)
S1	0.5000	0.0299 (3)	0.7500	0.0182 (4)
C1	0.3390 (2)	0.0272 (7)	0.9554 (4)	0.0134 (10)
C2	0.3697 (2)	0.2318 (7)	0.9654 (4)	0.0148 (10)
C3	0.3764 (2)	0.3838 (7)	1.0402 (4)	0.0145 (10)
C4	0.3492 (2)	0.4128 (7)	1.1340 (4)	0.0128 (10)
C5	0.4168 (2)	0.4805 (8)	0.9077 (4)	0.0179 (11)
H5	0.4371	0.5603	0.8664	0.022*
N1	0.3942 (2)	0.2930 (6)	0.8817 (3)	0.0165 (9)
N2	0.4065 (2)	0.5391 (6)	1.0009 (3)	0.0183 (10)
H1	0.420 (3)	0.648 (6)	1.039 (4)	0.027*
O1	0.32418 (19)	-0.0583 (5)	1.0318 (3)	0.0220 (9)
O2	0.32955 (18)	-0.0546 (5)	0.8633 (3)	0.0192 (8)
O3	0.33204 (18)	0.2591 (5)	1.1767 (3)	0.0219 (8)
O4	0.34067 (19)	0.5917 (5)	1.1620 (3)	0.0219 (8)
O5	0.45816 (18)	-0.0925 (5)	0.7997 (3)	0.0304 (10)
O6	0.45308 (19)	0.1572 (6)	0.6710 (3)	0.0349 (10)
O1W	0.24374 (18)	0.1038 (6)	0.6799 (3)	0.0250 (9)
H2W	0.224 (2)	0.201 (6)	0.646 (4)	0.037*
H1W	0.221 (3)	0.075 (8)	0.720 (4)	0.037*

### Atomic displacement parameters ( $\text{\AA}^2$ )

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
Yb1	0.01712 (13)	0.00743 (13)	0.00944 (13)	0.00016 (8)	0.00604 (9)	0.00022 (8)
S1	0.0156 (9)	0.0145 (9)	0.0250 (10)	0.000	0.0063 (8)	0.000
C1	0.017 (2)	0.010 (2)	0.012 (3)	0.0000 (19)	0.001 (2)	0.001 (2)
C2	0.021 (2)	0.012 (3)	0.011 (2)	-0.003 (2)	0.0040 (19)	0.000 (2)
C3	0.021 (3)	0.013 (2)	0.011 (2)	0.002 (2)	0.006 (2)	0.001 (2)
C4	0.017 (2)	0.010 (3)	0.010 (2)	-0.0018 (19)	0.002 (2)	-0.0017 (19)
C5	0.025 (3)	0.015 (3)	0.015 (3)	-0.005 (2)	0.008 (2)	0.003 (2)

## supplementary materials

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N1	0.024 (2)	0.012 (2)	0.016 (2)	-0.0023 (17)	0.0082 (18)	-0.0010 (17)
N2	0.027 (2)	0.014 (2)	0.016 (2)	-0.0064 (19)	0.0084 (19)	-0.0018 (18)
O1	0.042 (2)	0.0151 (19)	0.0107 (19)	-0.0090 (16)	0.0095 (17)	-0.0001 (15)
O2	0.033 (2)	0.0155 (19)	0.0110 (18)	-0.0084 (15)	0.0090 (15)	-0.0058 (15)
O3	0.037 (2)	0.0144 (19)	0.0182 (18)	0.0042 (16)	0.0134 (16)	0.0061 (16)
O4	0.039 (2)	0.0103 (19)	0.018 (2)	0.0028 (16)	0.0105 (17)	-0.0009 (14)
O5	0.021 (2)	0.030 (2)	0.041 (3)	0.0019 (16)	0.0104 (18)	0.0155 (19)
O6	0.023 (2)	0.044 (2)	0.041 (3)	0.0071 (19)	0.0135 (19)	0.027 (2)
O1W	0.024 (2)	0.023 (2)	0.031 (2)	0.0066 (17)	0.0129 (18)	0.0083 (17)

*Geometric parameters ( $\text{\AA}$ ,  $^\circ$ )*

Yb1—O4 <sup>i</sup>	2.264 (3)	C1—C2	1.481 (6)
Yb1—O1 <sup>ii</sup>	2.272 (3)	C2—C3	1.367 (7)
Yb1—O1W	2.280 (4)	C2—N1	1.377 (6)
Yb1—O3 <sup>ii</sup>	2.291 (3)	C3—N2	1.369 (6)
Yb1—O2	2.297 (3)	C3—C4	1.485 (7)
Yb1—O6	2.342 (4)	C4—O3	1.249 (6)
Yb1—O5	2.421 (4)	C4—O4	1.255 (5)
Yb1—N1	2.510 (4)	C5—N1	1.328 (6)
Yb1—S1	2.9798 (3)	C5—N2	1.334 (7)
S1—O5 <sup>iii</sup>	1.464 (4)	C5—H5	0.9300
S1—O5	1.464 (4)	N2—H1	0.87 (5)
S1—O6 <sup>iii</sup>	1.470 (4)	O1—Yb1 <sup>iv</sup>	2.272 (3)
S1—O6	1.470 (4)	O3—Yb1 <sup>iv</sup>	2.291 (3)
S1—Yb1 <sup>iii</sup>	2.9798 (3)	O4—Yb1 <sup>v</sup>	2.264 (3)
C1—O1	1.244 (6)	O1W—H2W	0.82 (2)
C1—O2	1.266 (6)	O1W—H1W	0.82 (6)
O4 <sup>i</sup> —Yb1—O1 <sup>ii</sup>	76.46 (12)	O6 <sup>iii</sup> —S1—O6	110.8 (4)
O4 <sup>i</sup> —Yb1—O1W	79.74 (14)	O5 <sup>iii</sup> —S1—Yb1	135.09 (15)
O1 <sup>ii</sup> —Yb1—O1W	78.99 (15)	O5—S1—Yb1	53.75 (14)
O4 <sup>i</sup> —Yb1—O3 <sup>ii</sup>	148.74 (13)	O6 <sup>iii</sup> —S1—Yb1	120.86 (16)
O1 <sup>ii</sup> —Yb1—O3 <sup>ii</sup>	74.75 (12)	O6—S1—Yb1	50.65 (15)
O1W—Yb1—O3 <sup>ii</sup>	83.05 (14)	O5 <sup>iii</sup> —S1—Yb1 <sup>iii</sup>	53.75 (14)
O4 <sup>i</sup> —Yb1—O2	124.73 (12)	O5—S1—Yb1 <sup>iii</sup>	135.09 (15)
O1 <sup>ii</sup> —Yb1—O2	140.73 (13)	O6 <sup>iii</sup> —S1—Yb1 <sup>iii</sup>	50.65 (15)
O1W—Yb1—O2	74.07 (14)	O6—S1—Yb1 <sup>iii</sup>	120.86 (16)
O3 <sup>ii</sup> —Yb1—O2	74.10 (12)	Yb1—S1—Yb1 <sup>iii</sup>	167.75 (7)
O4 <sup>i</sup> —Yb1—O6	76.89 (14)	O1—C1—O2	122.7 (4)
O1 <sup>ii</sup> —Yb1—O6	77.64 (14)	O1—C1—C2	122.6 (4)
O1W—Yb1—O6	150.11 (14)	O2—C1—C2	114.7 (4)
O3 <sup>ii</sup> —Yb1—O6	108.21 (14)	C3—C2—N1	110.6 (4)
O2—Yb1—O6	135.20 (13)	C3—C2—C1	132.9 (5)
O4 <sup>i</sup> —Yb1—O5	127.57 (13)	N1—C2—C1	116.5 (4)

O1 <sup>ii</sup> —Yb1—O5	114.21 (14)	C2—C3—N2	104.5 (4)
O1W—Yb1—O5	150.85 (13)	C2—C3—C4	132.8 (4)
O3 <sup>ii</sup> —Yb1—O5	76.28 (13)	N2—C3—C4	121.8 (4)
O2—Yb1—O5	80.58 (13)	O3—C4—O4	123.2 (5)
O6—Yb1—O5	58.02 (13)	O3—C4—C3	118.5 (4)
O4 <sup>i</sup> —Yb1—N1	72.99 (13)	O4—C4—C3	118.1 (4)
O1 <sup>ii</sup> —Yb1—N1	148.68 (12)	N1—C5—N2	111.0 (4)
O1W—Yb1—N1	101.95 (14)	N1—C5—H5	124.5
O3 <sup>ii</sup> —Yb1—N1	136.57 (13)	N2—C5—H5	124.5
O2—Yb1—N1	66.31 (12)	C5—N1—C2	105.0 (4)
O6—Yb1—N1	88.79 (15)	C5—N1—Yb1	138.2 (3)
O5—Yb1—N1	80.25 (14)	C2—N1—Yb1	113.6 (3)
O4 <sup>i</sup> —Yb1—S1	101.39 (10)	C5—N2—C3	109.0 (4)
O1 <sup>ii</sup> —Yb1—S1	98.30 (10)	C5—N2—H1	130 (4)
O1W—Yb1—S1	176.78 (11)	C3—N2—H1	121 (4)
O3 <sup>ii</sup> —Yb1—S1	94.59 (10)	C1—O1—Yb1 <sup>iv</sup>	141.5 (3)
O2—Yb1—S1	107.44 (9)	C1—O2—Yb1	127.3 (3)
O6—Yb1—S1	29.03 (9)	C4—O3—Yb1 <sup>iv</sup>	143.5 (3)
O5—Yb1—S1	29.18 (9)	C4—O4—Yb1 <sup>v</sup>	164.1 (3)
N1—Yb1—S1	81.27 (10)	S1—O5—Yb1	97.06 (18)
O5 <sup>iii</sup> —S1—O5	113.5 (3)	S1—O6—Yb1	100.32 (19)
O5 <sup>iii</sup> —S1—O6 <sup>iii</sup>	103.9 (2)	Yb1—O1W—H2W	121 (4)
O5—S1—O6 <sup>iii</sup>	112.4 (2)	Yb1—O1W—H1W	128 (4)
O5 <sup>iii</sup> —S1—O6	112.4 (2)	H2W—O1W—H1W	102 (3)
O5—S1—O6	103.9 (2)		

Symmetry codes: (i)  $x, -y+1, z-1/2$ ; (ii)  $x, -y, z-1/2$ ; (iii)  $-x+1, y, -z+3/2$ ; (iv)  $x, -y, z+1/2$ ; (v)  $x, -y+1, z+1/2$ .

#### *Hydrogen-bond geometry ( $\text{\AA}$ , $^\circ$ )*

$D\text{—H}\cdots A$	$D\text{—H}$	$H\cdots A$	$D\cdots A$	$D\text{—H}\cdots A$
N2—H1 $\cdots$ O6 <sup>v</sup>	0.87 (5)	2.09 (3)	2.925 (6)	161 (5)
O1W—H2W $\cdots$ O2 <sup>vi</sup>	0.82 (2)	1.94 (3)	2.693 (5)	151 (5)
O1W—H1W $\cdots$ O3 <sup>vii</sup>	0.82 (6)	2.24 (4)	2.896 (5)	138 (5)
O1W—H1W $\cdots$ O4 <sup>vii</sup>	0.82 (6)	2.51 (6)	3.308 (5)	167 (5)
C5—H5 $\cdots$ O5 <sup>viii</sup>	0.93	2.52	3.347 (6)	149.

Symmetry codes: (v)  $x, -y+1, z+1/2$ ; (vi)  $-x+1/2, y+1/2, -z+3/2$ ; (vii)  $-x+1/2, -y+1/2, -z+2$ ; (viii)  $x, y+1, z$ .

## supplementary materials

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Fig. 1

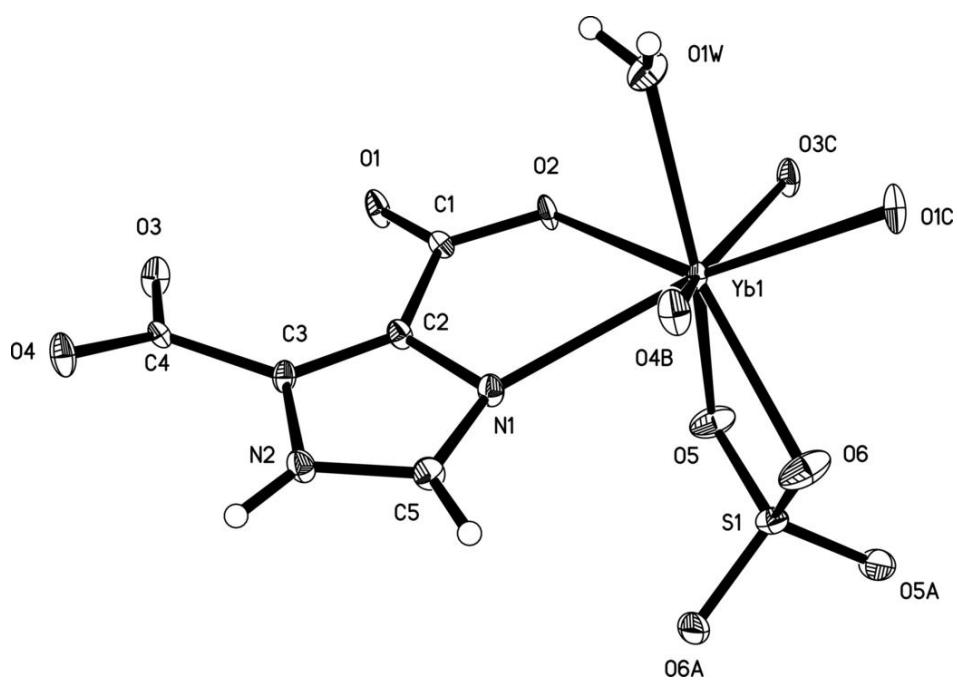


Fig. 2

